

EU HORIZON 2020 PROJECT STEP2DYNA SEMINAR Bio-inspired Neural System and Models



A Ring Attractor Model for Cues Integration

Xuelong Sun

Monday, 21 May 2018 Tsinghua University, Beijing



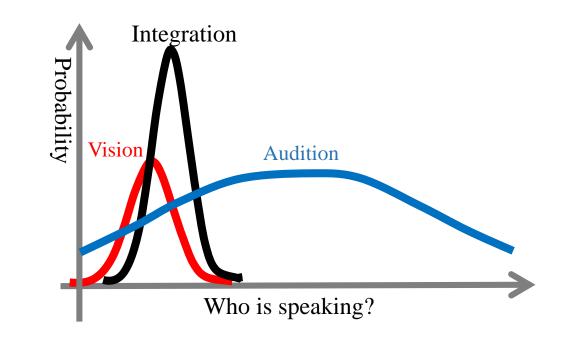


Background & Motivations

A fundamental principle underlying animal intelligence is the capacity to appropriately combine redundant sensory (e.g. **vision**, **olfactory and haptic**) of the same percept to achieve a **more accurate and robust estimate**.

Example 1:



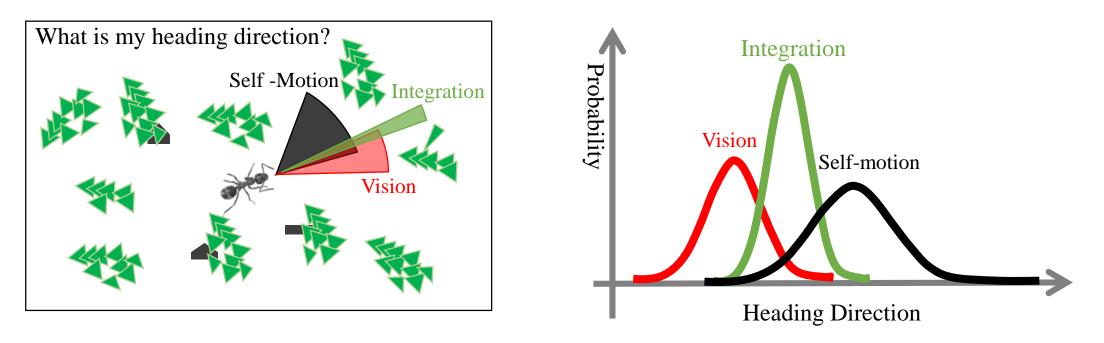


Shettleworth, S. J. (2010). Cognition, evolution, and behavior. Oxford University Press.



Background & Motivations

Example 2:



Bayesian Method:
$$P(x_{true} | x_{cue}) = P(x_{cue} | x_{true}) P(x_{true}) / P(x_{cue})$$

Maximum Likelihood Estimation: $\overline{X} = \sum_{i}^{n} W_{i}X_{i}, W_{i} = 1/\sigma_{i}^{2}/(\sum_{j}^{n} 1/\sigma_{j}^{2})$
Optimal integration!

How to do it in a biology plausible way? Shall we get inspiration from animals to robot applications?

Ernst, M. O., & Knoblich, G. (2006). A Bayesian view on multimodal cue integration. Human body perception from the inside out, 131, 105-131.



Heading Direction System and Ring Attractor

Insects encode the heading direction using ring neurons 0000 t = 113.4 s *t* = 1.8 s *t* = 33.3 s *t* = 38.1 s t = 43.4 st = 60.0 sD F 70 max 60 50 40 30 20 10 0 min $3\pi/4$ Cue 2 Cue 1 Winner-take-all Cue combination The Journal of Physiology

Rodents encode the heading direction using neurons

(although not arrange in a ring physically (c))

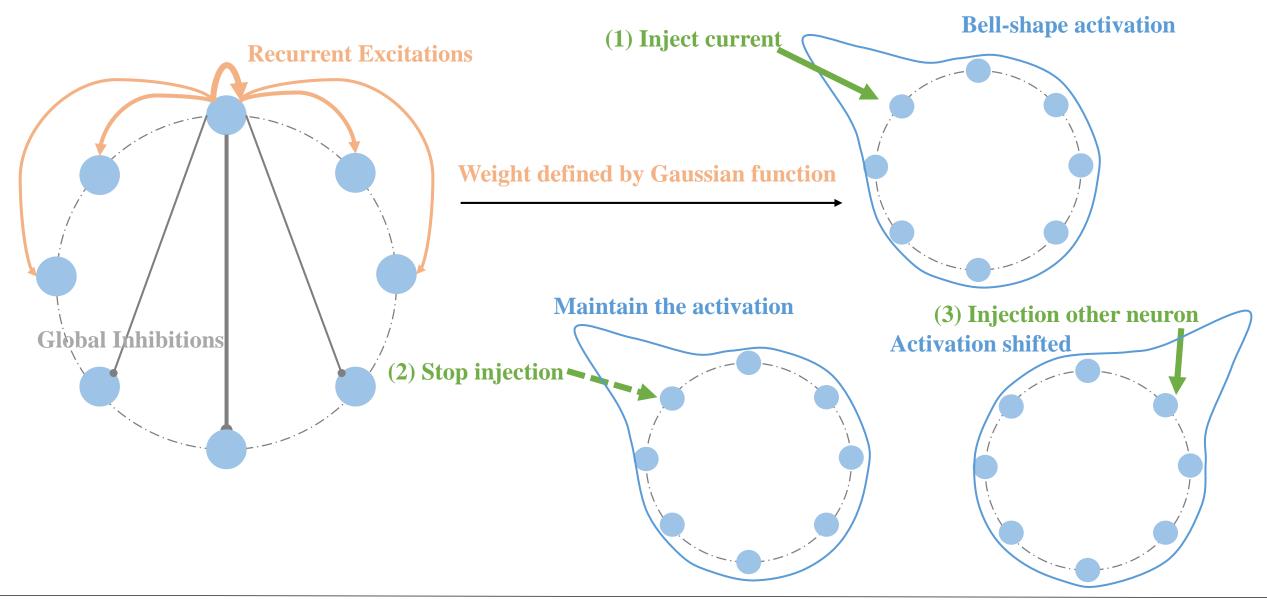
Both have the **ring attractor** properties

Seelig JD, Jayaraman V, Neural dynamics for landmark orientation and angular path integration, Nature 521(7551):186–191, 2015.

Jeery, K. J., Page, H. J., Stringer, S. M. (2016). Optimal cue combination and landmark-stability learning in the head direction system. The Journal of physiology, 594(22), 6527-6534

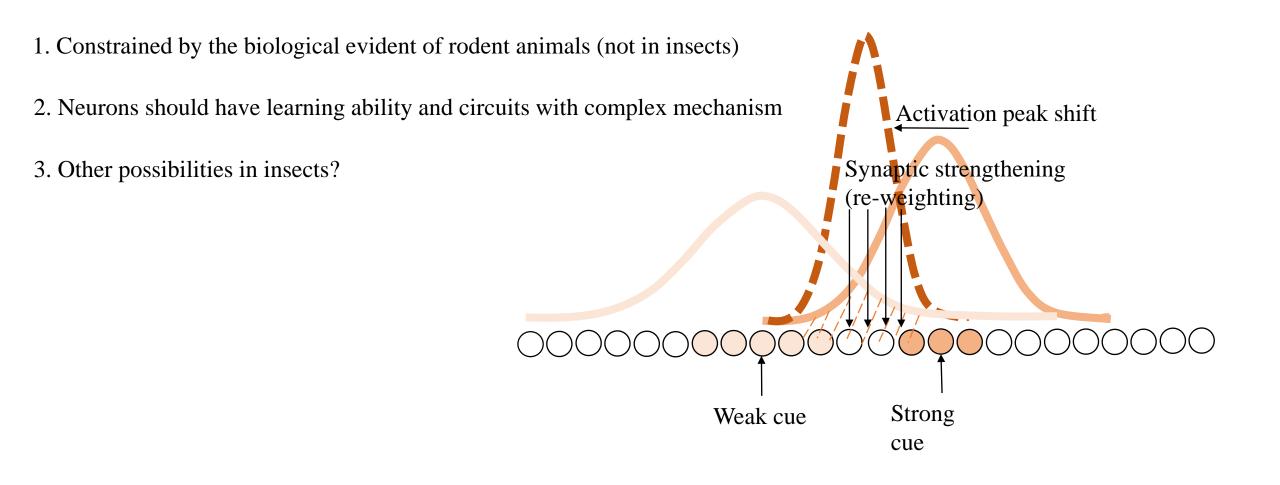


Ring Attractor Network



Touretzky, D. S. (2005). Attractor network models of head direction cells. Head direction cells and the neural mechanisms of spatial orientation, 411-432.

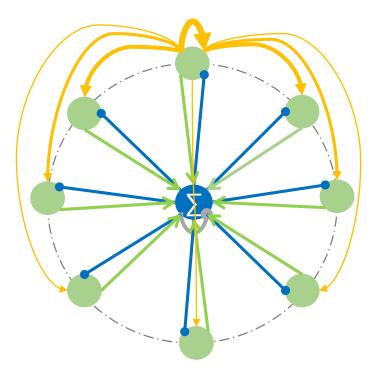




Jeery, K. J., Page, H. J., Stringer, S. M. (2016). Optimal cue combination and landmark-stability learning in the head direction system. The Journal of physiology, 594(22), 6527-6534



Our Model – Ring attractor without re-weighting



Touretzky ring attractor

Integration Neurons

Uniform Inhibition Neurons

- ----> Excitation Connections
- Inhibition Connections

All neurons are CTRNN neurons, so the membrane potential C_i

$$\tau \frac{dc_i}{dt} = -c_i + I_i$$

 I_i is the total current injected to the neuron

$$I_{i} = \sum_{j=1}^{n} W_{ij}O_{j} + X_{i} = \sum_{j=1}^{n} W_{ij}g(c_{i})X_{i}$$
$$g(c_{i}) = \max(0, \theta + c)$$

W is the connection weights, and the recurrent excitation weights is defined by the Gaussian function

$$W_{ii}^{E \to E} = e^{\frac{-d_{ji}^2}{2\sigma^2}}$$

 d_{ji} is the difference between the preference of i and j neuron

g is the activation function to guarantee the nonlinear property

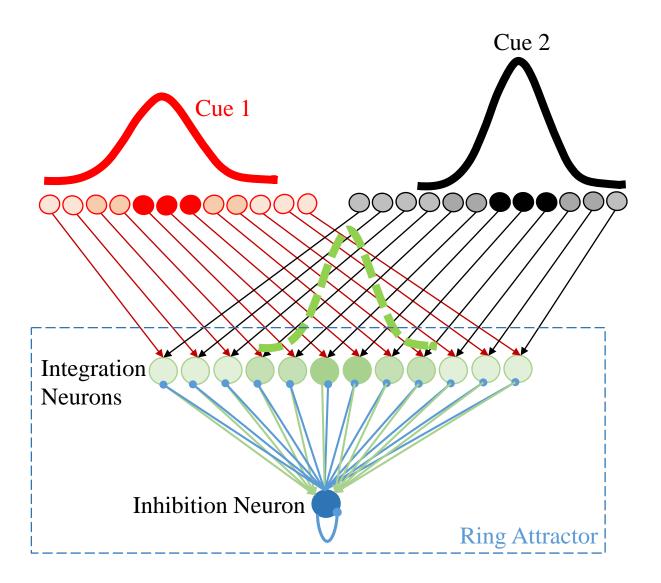
 X_i is the external input

The uniform inhibitory neuron sums all the integration activations and feedback the same inhibition to all the neurons

Touretzky, D. S. (2005). Attractor network models of head direction cells. Head direction cells and the neural mechanisms of spatial orientation, 411-432.



Our Model – Signals Processing



Cues are defined by the Gaussian function as:

$$F(i) = \frac{K}{\sqrt{2\pi\sigma}} e^{\frac{-(p_i - u)^2}{2\sigma^2}} + \xi N(0, 1)$$

We input the two cues at the same time, so the time evolution equation of the membrane potential of the integration neurons becomes:

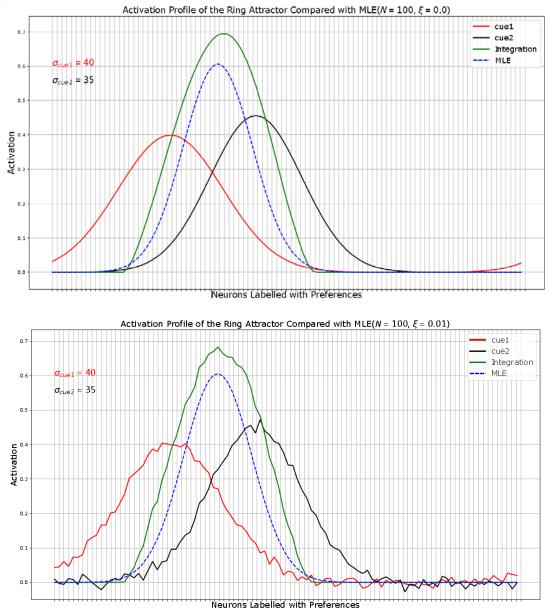
$$\tau \frac{dc_i}{dt} = -c_i + g(\sum_{j=1}^n W_{ji}^{E \to E} c_j + X \mathbf{1}_i + X \mathbf{2}_i + W^{I \to E} u)$$

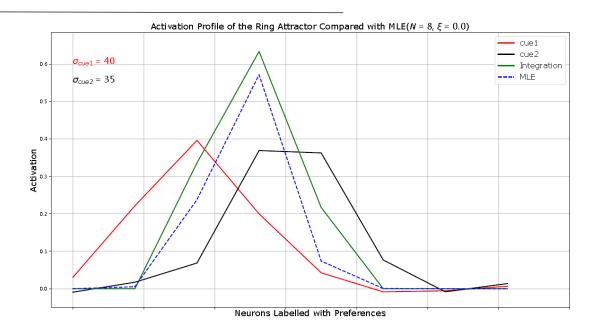
And the time evolution equation of uniform inhibition neuron is:

$$\tau \frac{du}{dt} = -u + g(W^{I \to I}u + W^{E \to I}\sum_{k=1}^{n} c_k)$$



Model Testing – Activation Profiles





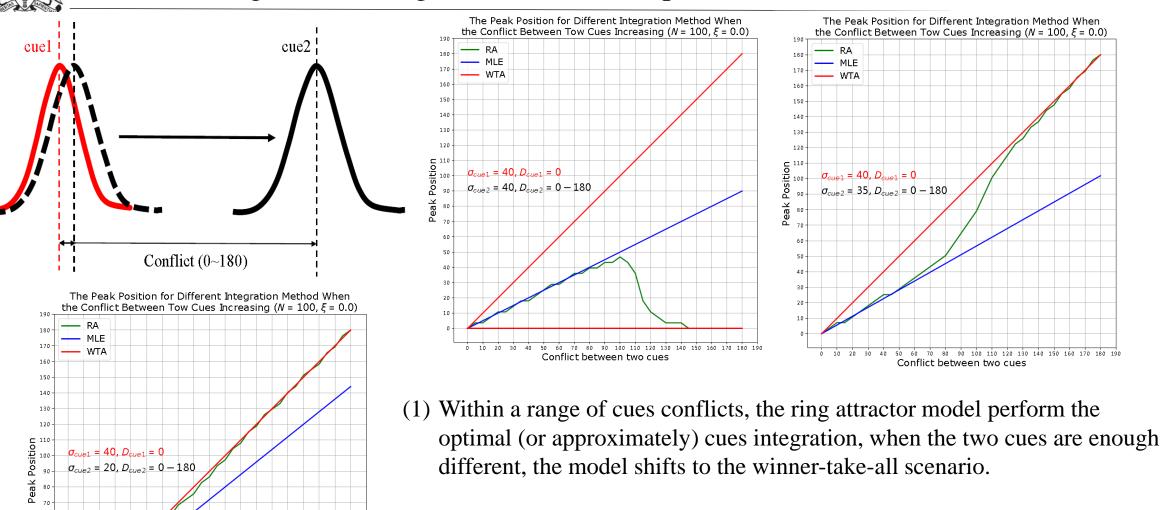
(1) Integration of conflicting cues by a ring attractor network shows that the response approaching the optimal integration.

(2) The model remained stable despite the white noise and obvious loss of resolution in the Gaussian functions.

Model Testing – Increasing the conflicts of input cues

20

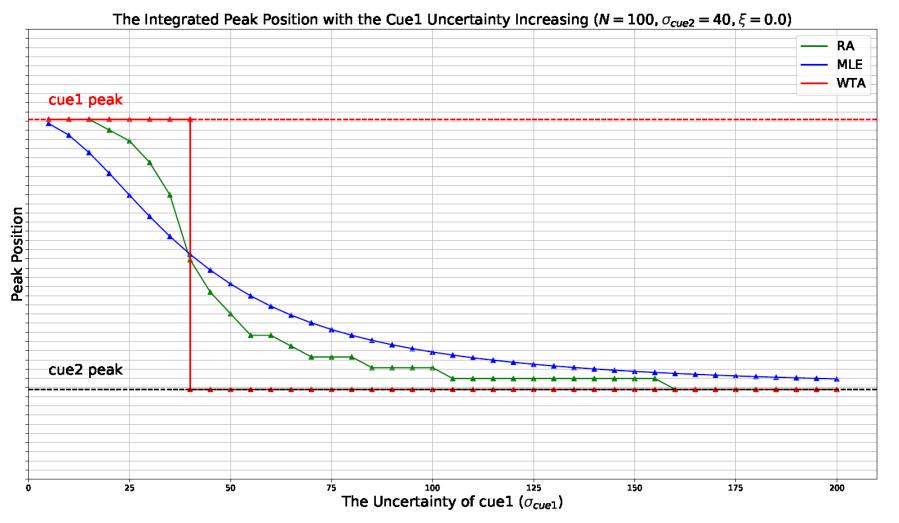
10 20 30 40 50 60 70 80 90 100 110 120 130 140 150 160 170 180 190 Conflict between two cues



(2) The difference between the uncertainty of two cues also strongly affect the model output.



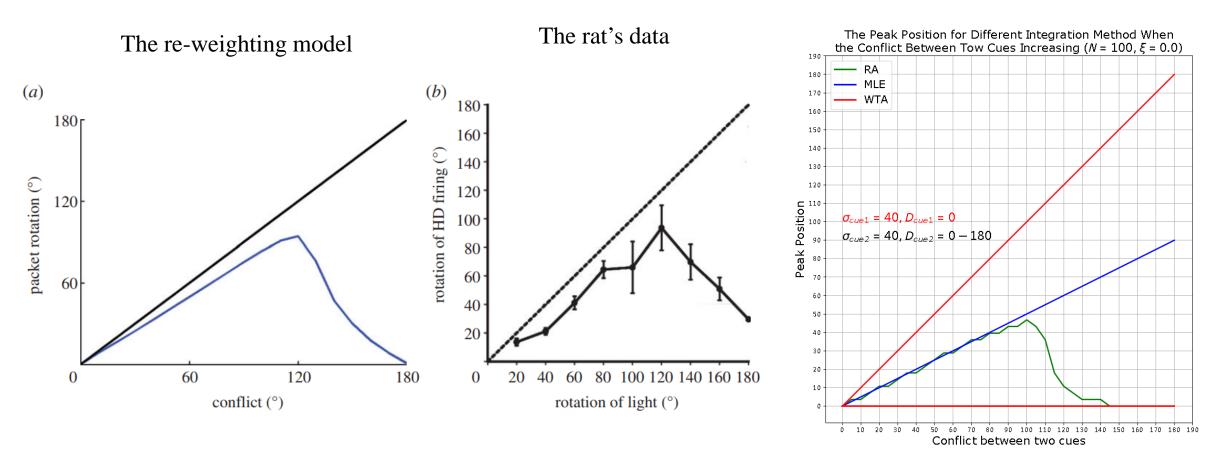
Model Testing – Altering the uncertainty of one cue



Although not acting in a truly optimal manner the switch from WTA to weighted-average and back again follows the general profile of the MLE prediction.



Discussion- Insect's performances?



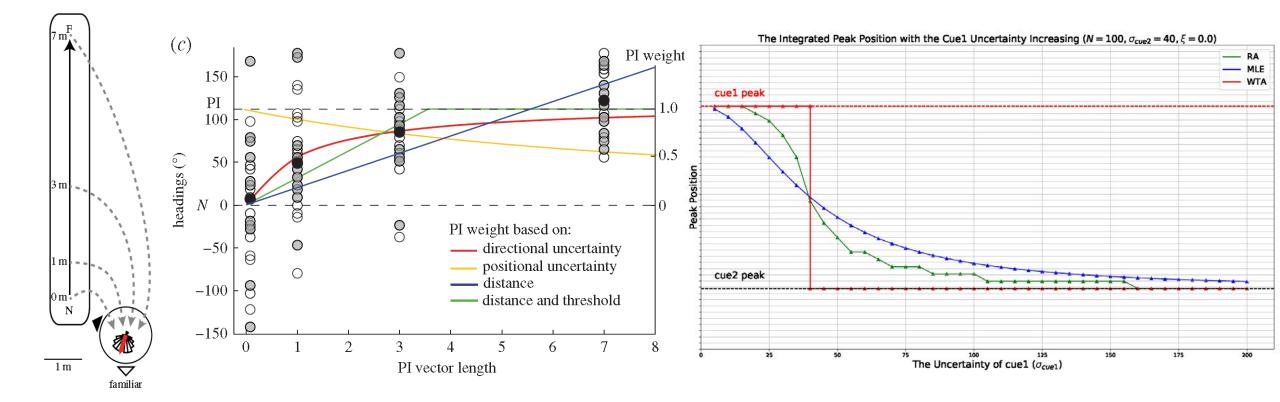
Have very similar performances as the re-weighting model and also the biological experiments.

Page, H. J., Walters, D. M., Knight, R., Piette, C. E., Jeery, K. J., & Stringer, S. M. (2014). A theoretical account of cue averaging in the rodent head direction system. Philosophical Transactions of the Royal Society B: Biological Sciences, 369(1635), 20130283.

Knight, R., Piette, C. E., Page, H., Walters, D., Marozzi, E., Nardini, M., ... & Jeery, K. J. (2014). Weighted cue integration in the rodent head direction system. Philosophical Transactions of the Royal Society of London B: Biological Sciences, 369(1635), 20120512.



Discussion- Insect's performances?

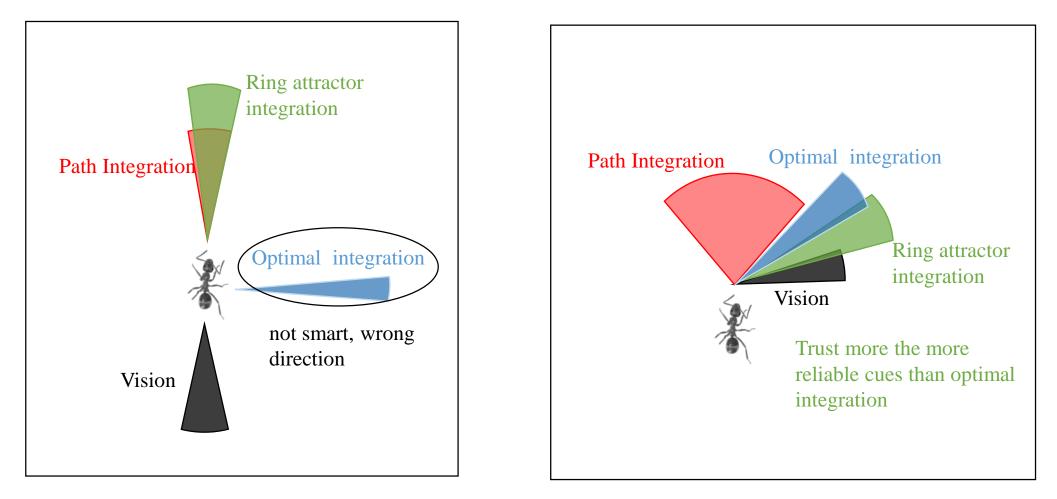


The tendency is very similar, some of the differences may be caused by the parameter setting.

Wystrach A, Mangan M and Webb B, Optimal cue integration in ants. Proc. R. Soc. B 282: 20151484. 2015.



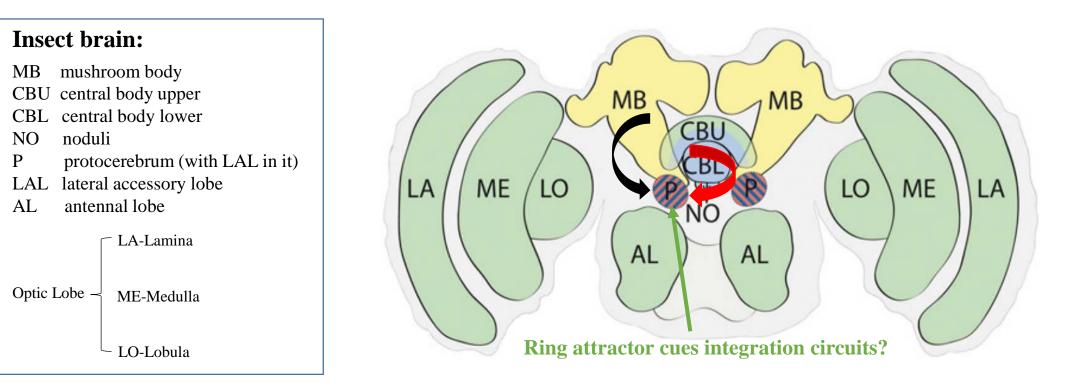
Discussion-Is optimal integration the best way?



The smartest way is when two cues are closed enough, we do the optimal integration and when two cues are disparted, choose the more reliable one and if they are identically reliable, arbitrarily select one. Ring attractor possesses this capacity with only a very simple network structure.



(1) Information integration in the LAL



(2) Other areas that needs information combining. Ring attractor network may be a ubiquitous circuits in animals' brain.



Sensory Fusion

(1) Can do the optimal-like integration

platforms Camera for Activation Profile of the Ring Attractor Compared with MLE($N = 8, \xi = 0.0$) cue1 environment $\sigma_{cue1} = 40$ Integration MLE matching algorithm $\sigma_{cue2} = 35$ Combining to get Activation more precious selfposition 0.2 Blanche Odometer for measuring Neurons Labelled with Preferences

(2) Cost very little computing resources (8 neurons can still work well),

make it possible for applying Bayesian method on small, cheap robot

Cox, I. J. (1991). Blanche-an experiment in guidance and navigation of an autonomous robot vehicle. IEEE Transactions on robotics and automation, 7(2), 193-204.

Kam, M., Zhu, X., & Kalata, P. (1997). Sensor fusion for mobile robot navigation. Proceedings of the IEEE, 85(1), 108-119.



Conclusions

- Our implementation of the classic ring attractor can perform optimal-like cue integration when presented with conflicting cues.
- The network output is also shown to be robust to noise on the sensory input and reduction in size to the 8 neurons that encode direction in insects.
- Sweep tests showed both the variance and distance between conflicting cues strongly affect the network properties.:

 With equal or small differences in variance of cues the network performs a weighted average for small cue conflicts, but switches to a winner-take-all response for larger conflicts.

(2) larger differences the network switches to WTA responses at much small conflicts.

- Simple ring attractor network possesses the capacity of smartly switching from optimal integration to winner-take-all shows a similar properties of animals' behavior supported by some biological experiments.
- With the advantage of small size and simple structure, it can be applied in small and cheap robot needing sensory fusion.



EU HORIZON 2020 PROJECT STEP2DYNA SEMINAR Bio-inspired Neural System and Models





Thank You!

Xuelong Sun

Monday, 21 May 2018 Tsinghua University, Beijing

